## Mathematics 5 SN

## Guide

Quadrilateral RSTU is a parallelogram and $M$ is the point of intersection of its diagonals.


Antoine lists the following vector operation statements:

1) $\overrightarrow{\mathrm{ST}}+\overrightarrow{\mathrm{SR}}=2 \overrightarrow{\mathrm{MU}}$
2) $\overrightarrow{\mathrm{UT}}+\overrightarrow{\mathrm{UR}}=2 \overrightarrow{\mathrm{SM}}$
3) $\overrightarrow{\mathrm{RS}}+\overrightarrow{\mathrm{RU}}=\overrightarrow{\mathrm{RT}}$
4) $\overrightarrow{\mathrm{MT}}+\overrightarrow{\mathrm{MR}}+\overrightarrow{\mathrm{MS}}+\overrightarrow{\mathrm{MU}}=\overrightarrow{0}$
5) $\overrightarrow{\mathrm{SR}}-\overrightarrow{\mathrm{ST}}=\overrightarrow{\mathrm{RT}}$

Which of these statements are true?
A) 1, 2 and 3 only
C) 2,4 and 5 only
B) 1,2 and 5 only
D) 1,3 and 4 only

2
Given the following information:

$$
\begin{aligned}
& \vec{a} \text { and } \vec{b} \text { are nonzero vectors in the plane } \\
& \vec{a} \neq \vec{b} \\
& k \text { is a scalar not equal to zero } \\
& k \neq 1
\end{aligned}
$$

Which of the following statements is true?
A) $\quad \mathrm{k}(\overrightarrow{\mathrm{a}} \bullet \overrightarrow{\mathrm{b}})=\mathrm{ka} \bullet \mathrm{k} \overrightarrow{\mathrm{b}}$
B) $k(\vec{a}+\vec{b})=k \vec{a}+k \vec{b}$
C) If $\overrightarrow{\mathrm{a}} \bullet \overrightarrow{\mathrm{b}}=0$ then $\overrightarrow{\mathrm{a}}$ and $\overrightarrow{\mathrm{b}}$ are collinear
D) If $\vec{a}=k \vec{b}$ then $\vec{a}$ and $\vec{b}$ are noncollinear

3 Given $\stackrel{\mu}{u}$ and $\stackrel{\mu}{v}$ two vectors that are not opposite.

Which of the following is FALSE?
А) $\underset{u}{\mu} \bullet \stackrel{\mu}{v}=\underset{v}{v} \bullet \underset{u}{u}$
с) $\quad 2(\vec{u}+\hat{v})=2 k+2 k$
B) $\quad 2 \mu \bullet 3 k=6 k \bullet u$
D) $\quad 2 \hat{u}+3 \hat{v}=3 \hat{u}+2 \hat{v}$

Given the following prism having a rectangular base.


Which vector is equivalent to the resultant of the expression $\overrightarrow{\mathbf{A D}}+\overrightarrow{\mathbf{H E}}+\overrightarrow{\mathbf{A E}}$ ?
A) $\overrightarrow{\mathrm{DH}}$
c) $\quad \overrightarrow{\mathrm{FB}}$
B) $\overrightarrow{\mathrm{BE}}$
D) $\overrightarrow{\mathrm{BC}}$

The Egyptians used an ingenious pulley system to move the blocks of stone used in the construction of pyramids. To minimize the work needed to displace the blocks, they applied a force oriented at $26^{\circ}$. (Work $(\mathrm{Nm})$ is the scalar product of the force vector and the displacement vector.)


Rounded to the nearest Nm , what work is needed to displace a block of stone horizontally for a distance of 200 m , if the force applied to it is 1500 N oriented at $26^{\circ}$ ?
A) $\quad 131511 \mathrm{Nm}$
B) $\quad 194076 \mathrm{Nm}$
C) $\quad 228768 \mathrm{Nm}$
D) 269638 Nm

The following figure represents a right prism.


Which of these statements is FALSE?
A) $\quad \overrightarrow{\mathrm{BC}}+\overrightarrow{\mathrm{GF}}=\overrightarrow{0}$
B) $\overrightarrow{\mathrm{AB}}-\overrightarrow{\mathrm{FE}}=\overrightarrow{0}$
C) $\quad \overrightarrow{\mathrm{AB}} \bullet \overrightarrow{\mathrm{AD}}=0$
D) $\overrightarrow{\mathrm{EH}}+\overrightarrow{\mathrm{HF}}+\overrightarrow{\mathrm{FG}}-\overrightarrow{\mathrm{EG}}=\overrightarrow{0}$

7
Given the three vectors $u, v$, and $w$.

$$
\begin{aligned}
& \vec{v}=(-2,-3) \\
& \vec{u} \text { and } \vec{w} \text { are represented in the Cartesian plane below: }
\end{aligned}
$$



Which of the following statements is TRUE?
A) $\vec{v}$ and $-\vec{u}$ are opposite.
B) $\quad \vec{u}$ and $\vec{v}$ are equivalent.
C) $\quad \vec{w}$ and $(\vec{v}+\vec{w})$ are perpendicular.
D) $\quad \vec{u}$ and $3 \vec{v}$ are collinear.


Which of the following statements is FALSE?
A) $\quad \overrightarrow{\mathrm{PQ}}+\overrightarrow{\mathrm{QR}}=\overrightarrow{\mathrm{PR}}$
B) $\quad \overrightarrow{\mathrm{RP}}-\overrightarrow{\mathrm{SP}}=\overrightarrow{\mathrm{RS}}$
C) $\quad \overrightarrow{\mathrm{PS}}+\overrightarrow{\mathrm{SR}}=\overrightarrow{\mathrm{RP}}$
D) $\quad \overrightarrow{\mathrm{SQ}}+\overrightarrow{\mathrm{QR}}+\overrightarrow{\mathrm{RS}}=\overrightarrow{\mathrm{O}}$

9 Consider rectangle ABCD shown below.


Which of the following statements is true?
A) $\overrightarrow{\mathrm{DA}}+\overrightarrow{\mathrm{AB}}=\overrightarrow{\mathrm{AC}}$
B) $\overrightarrow{\mathrm{AB}} \cdot \overrightarrow{\mathrm{BC}}=\overrightarrow{\mathrm{AC}}$
C) $\overrightarrow{\mathrm{AB}} \cdot \overrightarrow{\mathrm{BC}}=\overrightarrow{\mathrm{DC}}+\overrightarrow{\mathrm{CB}}$
D) $\overrightarrow{\mathrm{AB}} \cdot \overrightarrow{\mathrm{AD}}=\overrightarrow{\mathrm{AB}} \cdot \overrightarrow{\mathrm{BC}}$

Given vectors $\vec{u}=(-3,9), \vec{v}=(6,2), \vec{w}=(6,-18)$ and $k \neq 0$.

Which of the following statements is FALSE?
A) $k \vec{u}+k \vec{v}=k(\vec{u}+\vec{v})$
B) $\quad k \vec{v} \cdot k \vec{w}=k(\vec{v}+\vec{w})$
C) $\quad \vec{u}$ and $\vec{w}$ are collinear.
D) $\quad \vec{u}$ and $\vec{v}$ are orthogonal.

The magnitudes of two vectors are 12 and 16 respectively, and their directions differ by 60 degrees.

What is the magnitude of the resultant of these two vectors?
A) -96
C) 24.34
B) $\quad 14.42$
D) 96

Given vectors $\vec{u}(1,-2), \vec{v}(3,-4)$ and $\vec{w}(5,6)$.

What is the resultant of the following expression?

$$
(2 \vec{u}+\vec{v}) \bullet \vec{w}
$$

A) -32
B) -23
C) 23
D) 73

Given the figure on the right in which:

- $\overline{\mathrm{AE}} / / \overline{\mathrm{CD}}$
- $\overline{\mathrm{AC}} / / \overline{\mathrm{ED}}$

- $\overline{\mathrm{AC}} \perp \overline{\mathrm{CD}}$

Consider the following 5 statements about figure $A B C D E$ :

1) $\overrightarrow{\mathrm{AB}}+\overrightarrow{\mathrm{BC}}=\overrightarrow{\mathrm{AC}}$
2) $\overrightarrow{\mathrm{EA}}+\overrightarrow{\mathrm{CD}}=\overrightarrow{0}$
3) $\overrightarrow{\mathrm{AB}}+\overrightarrow{\mathrm{AB}}=2 \overrightarrow{\mathrm{BC}}$
4) $\overrightarrow{\mathrm{EA}}=-\overrightarrow{\mathrm{AE}}$
5) $\overrightarrow{\mathrm{AC}}+\overrightarrow{\mathrm{DO}}=\overrightarrow{\mathrm{OE}}$

Which of the statements are true?
A) 1, 2 and 3
C) 2,4 and 5
B) 1, 2 and 4
D) 3,4 and 5

Given that $u$ and $v$ are vectors, which of the following is NOT a vector?
A) $\vec{u}+\vec{v}$
B) $\quad \vec{u}-\vec{v}$
C) $\quad \vec{u} \bullet \vec{v}$
D) $\quad 2(\vec{u}+\vec{v})$

Given $\vec{a}$ and $\vec{b}$, two vectors illustrated below.


Which one of the following diagrams illustrates the relation between $\vec{a}$ and $\vec{b}$ and $\vec{r}$, the resultant vector?
A)

C)

B)

D)


An airplane flying East at $150 \mathrm{~km} / \mathrm{h}$ encounters a $50 \mathrm{~km} / \mathrm{h}$ wind blowing in a $30^{\circ}$ East of North direction.

What will be the airplane's resultant velocity?
A) $\quad 180 \mathrm{~km} / \mathrm{h}\left[\mathrm{E} 14^{\circ} \mathrm{N}\right]$
B) $\quad 195 \mathrm{~km} / \mathrm{h}\left[\mathrm{E} 7^{\circ} \mathrm{N}\right]$
C) $\quad 200 \mathrm{~km} / \mathrm{h}\left[\mathrm{N} 30^{\circ} \mathrm{E}\right]$
D) $\quad 132 \mathrm{~km} / \mathrm{h}\left[\mathrm{E} 19^{\circ} \mathrm{S}\right]$

Given $\quad \overrightarrow{\mathrm{u}}=(3,2)$, and $\overrightarrow{\mathrm{v}}=(1,-4)$

What are the components of the resultant of the following vector operation?

$$
\overrightarrow{\mathrm{u}}-2 \overrightarrow{\mathrm{v}}
$$

A) $(1,10)$
B) $(1,-6)$
C) $(2,6)$
D) $(5,-6)$

Given vectors $\vec{U}$ and $\vec{v}$ shown below.


Which of the following vectors represents the resultant, $r$, of $\vec{u}-\vec{v}$ ?
A)

C)

B)

D)



Which proposition is TRUE?
A) $\overrightarrow{\mathrm{AB}}+\overrightarrow{\mathrm{BC}}+\overrightarrow{\mathrm{CD}}=\overrightarrow{\mathrm{DA}}$
B) $\overrightarrow{\mathrm{AB}}+\overrightarrow{\mathrm{BC}}=\overrightarrow{\mathrm{CD}}+\overrightarrow{\mathrm{DA}}$
C) $\quad \overrightarrow{\mathrm{AB}}+\overrightarrow{\mathrm{BC}}=-(\overrightarrow{\mathrm{DA}}+\overrightarrow{\mathrm{AB}})$
D) $\overrightarrow{\mathrm{AB}}+\overrightarrow{\mathrm{CD}}=\overrightarrow{0}$

Vector $u=(2,-5)$ makes an angle of $40^{\circ}$ with vector $v$ whose magnitude is 7.8 units.

To the nearest tenth, what is the scalar product (dot product) of $\overrightarrow{\boldsymbol{u}}$ and $\overrightarrow{\boldsymbol{v}}$ ?
A) $\quad 27.0$ units
B) $\quad 27.4$ units
C) 32.2 units
D) 42.0 units

21 Consider vectors $u$ and $v$ and constant $k$.

Which of the following is a scalar?
A) $k(\vec{u}+\vec{v})$
B) $\quad \vec{v}(\vec{u} \bullet \vec{v})$
C) $\quad k \vec{u}$
D) $\quad k(\vec{u} \bullet \vec{v})$

Consider vectors $v$ and $s$ below.


What is the resultant vector of $\vec{v}-\vec{s}$ ?
A)


B)

D)



Which of the following is the resultant, $\vec{u}+\vec{v}$ ?
A)

C)

B)

D)


## 2- Correction key

1 D
2 B
3 D


5 D


7 D
8 C

## 9 D

10 B

11 C

12 B

13 B

14 C

15 C

16 A

## 17 <br> A

18 B

19 D
$20 \quad C$

21 D

22 C

23 A

