

## EXERCISES

Find dot products of the following vectors.

1)  $\vec{u} = (-4, 3)$  and  $\vec{v} = (2, 5)$       2)  $\vec{v} = (0, 2)$  and  $\vec{u} = (6, -7)$     3)  $\vec{w} = (0, 4)$  and  $\vec{v} = (-7, 0)$

Let  $\vec{u} = (4, -6)$ ,  $\vec{v} = (-7, -3)$ ,  $\vec{w} = (2, -1)$ . Find

4)  $\vec{u} \cdot \vec{v}$       5)  $(2\vec{u}) \cdot \vec{v}$       6)  $\vec{u} \cdot (4\vec{v})$       7)  $(2\vec{u}) \cdot (3\vec{v})$       8)  $(2\vec{v}) \cdot (3\vec{u})$   
 9)  $(2\vec{u} + \vec{v}) \cdot \vec{u}$       10)  $(3\vec{u} + \vec{v}) \cdot (\vec{u} - \vec{v})$       11)  $(\vec{u} - 2\vec{v} + \vec{w}) \cdot (\vec{w} + \vec{v})$       12)  $(\vec{v} \cdot \vec{w}) \vec{u}$

Are the following vectors perpendicular?

13)  $\vec{u} = (3, -4)$  and  $\vec{v} = (8, 6)$       14)  $\vec{w} = (2, -1)$  and  $\vec{u} = (-4, -6)$   
 15)  $\vec{w} = (-2, -1)$  and  $\vec{v} = (3, -6)$       16)  $\vec{v} = (-2, 1)$  and  $\vec{u} = (-7, 4)$

For which value(s) of  $x$  the vectors  $\vec{u}$  and  $\vec{v}$  are perpendicular?

17)  $\vec{u} = (x, -2)$  and  $\vec{v} = (3, 6)$       18)  $\vec{u} = (x-1, 1)$  and  $\vec{v} = (x, x-1)$

Find the angle between vectors  $\vec{u}$  and  $\vec{v}$ .

19)  $\vec{u} = (1, -3)$ ,  $\vec{v} = (2, -1)$       20)  $\vec{u} = (1, \sqrt{3})$ ,  $\vec{v} = (-2, 0)$       21)  $\vec{u} = (6, -3)$ ,  $\vec{v} = (2, 4)$

Find the cosine of the angle between  $\vec{u} = (-2, 1)$  and  $\vec{v} = (3, -5)$  and then use a calculator to approximate the angle.

22)  $\vec{u} = (3, 4)$ ,  $\vec{v} = (5, -2)$       23)  $\vec{u} = (1, 5)$ ,  $\vec{v} = (-3, -1)$       24)  $\vec{u} = (0, -3)$ ,  $\vec{v} = (-1, 2)$

## Answers

- |         |              |         |
|---------|--------------|---------|
| 1) 7    | 2) -14       | 3) 0    |
| 4) -10  | 5) -20       | 6) -40  |
| 9) 94   | 10) 118      | 11) -96 |
| 13) yes | 14) no       | 15) yes |
| 17) 4   | 18) 1 and -1 | 16) no  |

19)  $\theta = 45^\circ$     20)  $\theta = 120^\circ$     21)  $\theta = 90^\circ$     22)  $\cos \theta = \frac{7}{5 \cdot \sqrt{29}}$ ,  $\theta \approx 74.93^\circ$

23)  $\cos \theta = \frac{-8}{\sqrt{26} \cdot \sqrt{10}} = \frac{-4}{\sqrt{13} \cdot \sqrt{5}}$ ,  $\theta \approx 119.74^\circ$     24)  $\cos \theta = \frac{-6}{3 \cdot \sqrt{5}} = \frac{-2}{\sqrt{5}}$ ,  $\theta \approx 153.43^\circ$